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## Mathematics and Information, Exercise sheet 11

Problem 1: (10 points) In the mini web

1	$\leftarrow$	2	$\rightarrow$	3
$\downarrow$		$\uparrow$	$\nearrow$	Î
4	$\leftarrow$	5	$\stackrel{\leftarrow}{\rightarrow}$	6
$\downarrow$	$\searrow$	$\downarrow$	,	$\downarrow$
7	$\rightarrow$	8	$\leftarrow$	9

somebody submits a query consisting of only one term, and this term only occurs in document one.

- a) Which part of the web will be considered after one, two, and three iterations?
- b) Recursively determine the authority and the hub weights of the nine documents for the whole collection!

## Problem 2: (10 points)

Some collection contains six documents, in which the following words occur with frequencies given in parenthesis:

- D<sub>1</sub>: Shannon (7), Entropy (1), Information (2) Cryptanalysis (1)
- D<sub>2</sub>: Shannon (1), Boltzmann (1), Entropy (8), Information (5)
- D<sub>3</sub>: Boltzmann (2), Entropy (4), Clausius (1), Information (3)
- D<sub>4</sub>: Boltzmann (5), Entropy (1), Clausius (1), Heat (5)
- D<sub>5</sub>: Information (4), Shannon (2), Code (6), Cryptanalysis (3), Key (4)
- $D_6$ : Kelly (5), Shannon (1), Bet (6), Portfolio (8), Information (3)
- D<sub>7</sub>: Las Vegas (5), Shannon (3), Kelly (1)
- $D_8$ : Shannon (20), Juggling (2), Roboter (4), Unicycle (1)
- a) Determine the global weight of each term using first the entropy based definition, and then the inverse document frequency!
- b) Compute the local weight of the term Shannon in these eight document, using the different definitions introduced in the course!
- c) Determine the first and the last column of the term document matrix for each of these definitions and the entropy based global weight!
- d) Determine the relevance of documents one and eight with respect to the queries Shannon and Shannon information!